

SWLDA OFFERS A VALUABLE TRADE-OFF BETWEEN INTERPRETABILITY AND ACCURACY FOR REHABILITATIVE BCIS

E. Colamarino^{1,2}, T. Colombo¹, F. Pichiorri², D. Mattia², L. Palagi¹, F. Cincotti^{1,2}

¹ Department of Computer, control, and management engineering Antonio Ruberti, Sapienza, University of Rome, Italy

² Neuroelectrical Imaging and BCI Lab, Fondazione Santa Lucia IRCCS, Rome, Italy

emma.colamarino@uniroma1.it

ABSTRACT: Interpretability, accuracy and a solid neurophysiological basis can be considered as the main requirements for the classification model to monitor motor imagery tasks in post-stroke motor recovery paradigms supported by the brain-computer interface technology.

This study aimed at comparing the accuracy performance of different classification approaches applied on a dataset of 15 stroke patients. We also explored how the variation in the dimensionality of the feature domain would influence the different classifier performance.

To this purpose, stepwise linear discriminant analysis (SWLDA), shrinkage linear discriminant analysis, logistic regression, support vector machine, multilayer perceptron, decision tree and random forest classifiers entered in the performance analysis.

SWLDA statistically outperformed the classifiers commonly used in sensorimotor-BCI paradigms, achieving 80% in classification accuracy even in case of feature domain dimensionality reduction. The linearity, the interpretability and the accuracy of the SWLDA model, even just by means few EEG electrodes, yielded to consider SWLDA an optimal solution to fulfil the main requirements of the rehabilitation context.

INTRODUCTION

Electroencephalogram (EEG)-based brain-computer interfaces (BCIs) have been recently proposed to assist motor recovery training in stroke patients [1], [2]. In this context two main approaches have been identified: the first employs brain activity to control devices to assist movement [1], the second aims at modifying brain activity to improve motor behaviour [2].

In [2], BCIs monitor the modulation of brain activity induced by the movement imagination. Indeed, motor imagery (MI) practice as well as motor execution elicits event-related desynchronization that occurs within EEG frequency bands (alpha and beta) and primarily over the scalp in sensorimotor cortical regions contralateral to the part of the body involved in the task. Therefore, the rationale behind such BCI approach is based on the assumption that the practice of mental imagery with motor content could influence brain plasticity and thus, enhance post-stroke functional motor recovery.

Although many approaches have already been proposed to detect and classify EEG signals [3], i.e. sensorimotor rhythms (SMR), classification algorithms are still being investigated. Low signal-to-noise ratio of EEG signals, their non-stationarity over time and the limited amount of training data available to calibrate the classifiers are the main challenges faced by classification methods for BCI [4].

In the context of SMR classification, although a survey of classifiers' performances has been already approached [3], no conclusive results were achieved because of the different context, i.e. different set of subjects, set of features and parameters, in which the studies took place. To overcome that limitation, Bashashati et al. [5] built a unified comparison framework to evaluate the performance of different classifiers (two feature extraction methods and seven classification methods) on several sensorimotor BCI dataset collected from healthy subjects. Multilayer perceptron, logistic regression, support vector machine and linear discriminant analysis classifiers resulted in the best performance in synchronous BCI paradigms. Moreover, the authors concluded that, since pre-processing of the data, feature extraction and feature selection all change the distribution of the data in the feature space, a BCI system should be viewed as a unit consisting of different blocks in which all the block settings and parameters should be adjusted jointly for each individual subject.

In contrast to other fields of application where optimal control is pursued, in the rehabilitation context the aim is also to reinforce the appropriate sensorimotor activation in terms of both topographical and spectral characteristics. Therefore, physiological constraints should be considered in the classification process to take into account neurophysiological evidences and rehabilitation principles.

In [2], neurologists selected the proper EEG features, i.e. BCI control parameters, basing on the visualization of EEG pattern in form of statistical index matrix obtained by the comparison between two conditions (task and rest). Those features and their weights (conventionally fixed to -0.5) were merged in a linear classifier.

From this approach, we have recently moved toward a semiautomatic selection, based on physiological constraints, able to reproduce the choices of neurologists [6]. The possibility to combine a proper feature selection

and a linear classifier (fast and powerful in interpretative terms) led us to apply the stepwise linear discriminant analysis [7], [8].

Since the specific rehabilitative context and the neurophysiological constraints, this study aimed to compare our classification approach and those proposed for the classification of sensorimotor rhythms. The experimental group, 15 stroke patients, made unique this analysis. Seven classification methods were compared, even on varying of the feature space size (two, ten or all available features). The methods, proposed in [5] as the best for synchronous BCI paradigms, i.e. the linear discriminant analysis, the logistic regression, the support vector machine and the multilayer perceptron were considered. The random forest classifier and its elementary module, the decision tree, were included in the comparative framework because of good classification performance achieved by the former [9] in binary classification of imaginative tasks.

MATERIALS AND METHODS

Data collection: EEG data were previously collected from fifteen stroke subjects according the procedure and the protocol in [2]. Scalp EEG potentials were acquired from 61 electrodes, assembled on an electrode cap (according to an extension of the 10–20 International System, linked ears reference, mastoid ground) and bandpass filtered between 0.1 and 70Hz.

All signals were digitalized at 200 Hz and amplified by a commercial EEG system (BrainAmp; Brain Products, Gilching, Germany).

Experimental protocol: During the acquisition all subjects were comfortably seated in an armchair in a dimly lit room with their upper limbs resting on a desk. Visual cues were presented on a screen on the desk.

All subjects were trained to perform the kinesthetic motor imagery of the hand movements (grasping and finger extension) with their affected upper limbs. Each run comprised 30 trials (15±1 rest, 15±1 motor imagery). The total duration of each trial was 7 seconds with an inter-trial interval of 3.5 seconds. In each trial the experimental task took up just 4 seconds.

Pre-processing and Feature Extraction: Runs collected during the motor imagery of grasping and finger extension movements were concatenated.

EEG data were notch filtered at 50 Hz. EEG signal intervals containing artefacts (muscular, environmental) were identified, using a semi-automatic procedure based on the definition of a voltage threshold, and discarded. EEG data were spatial filtered by means the common average reference spatial filter.

EEG data were divided into epochs 1 second long and spectral features were extracted using the maximum entropy method (16th order model, 2 Hz resolution, no overlap) [10]. Two hundred and forty epochs were at most available for each dataset (one for each subject).

Given the specific motor rehabilitation context, spectral features belonging to the sensorimotor strip (i.e. FC, C, CP electrodes) in the contralateral scalp area to the hand

involved in the task and in the range from 7 Hz to 25 Hz were used for the following steps.

After extracting features from each relevant channel (i.e. FC, C, CP in the affected hemisphere, 12 channels) and frequency bin (10 frequency bins), the features were assembled to build a feature vector, which was supplied to each classifier.

Feature selection: All classifiers were tested, even on varying of the feature number. Two features, ten features and all features (120 features) were considered.

To select the best two or ten features the recursive feature elimination cross-validation approach was used [11].

Recursive feature elimination (RFE) is a feature selection method that fits a model and removes the weakest features until the required number of features is reached. Features are ranked by the model's attributes, and by recursively eliminating a small number of features per loop, RFE attempts to eliminate dependencies and collinearity existing in the model. To find the optimal number of features, cross-validation strategy is applied. RFE cross-validation (RFECV) scores different feature subsets and selects the best scoring collection of features. In our approach the number of folds for the cross-validation was set to 3. Although in its first formulation RFE was applied jointly with the support vector machine (SVM) [11], we opted for the decision tree (DT) as estimator. The choice was based on the best classification results obtained in the comparison between SVM and DT as estimators. For conciseness, results of those analyses were not reported in this work.

RFECV was applied before all classifiers with the exception of the stepwise linear discriminant analysis, since the last intrinsically includes a feature selection process. This process can be controlled by the experimenter in term of number of features to be selected. As above reported, two or ten features was set also for the stepwise linear discriminant analysis.

Classification: Seven classifiers were compared in terms of classification performance.

Stepwise linear discriminant analysis (SWLDA) is an extension of the Fisher's Linear Discriminant that performs feature space reduction by selecting suitable features to be included in the discriminant function. In this classifier, a combination of forward and backward stepwise analysis is implemented. The input features are weighted using the Fisher's Linear Discriminant to predict the target labels. Starting with an empty model, the most statistically significant input feature for predicting the target label (having a p-value < 0.05) is added to the discriminant function. After each new entry to the discriminant function, a backward stepwise analysis is performed to remove the least significant features, having a p-value > 0.1. This process is repeated until the discriminant function includes a predetermined number of features, or until no additional features satisfy the entry/removal criteria [7].

Shrinkage linear discriminant analysis (sLDA) is a standard linear discriminant analysis (LDA) classifier in which the class-related covariance matrices used in its optimization have been regularized using shrinkage. The

sLDA classifier has been demonstrated to be more effective and more robust for small dataset than LDA [4]. In our implementation, the optimal shrinkage parameter was determined following the lemma introduced by Ledoit and Wolf.

Logistic regression (LR) is a discriminative learning classifier that directly estimates the parameters of the posterior distribution function. The maximum likelihood method is used to approximate such parameters [12]. In our implementation, the regularized logistic regression was optimized by means the liblinear [13] algorithm that supports both L1 and L2 regularization.

Support vector machine (SVM) is a classifier that uses a discriminant hyperplane to identify classes. The selected hyperplane is the ones that maximizes the distance (margin) from the nearest data points (support vectors) of each class [12]. In this study, we implemented the linear SVM and set the penalty parameter to $c=1$. Before selecting the value, three values ($c=0.1$, $c=1$ and $c=10$) were tested. No statistically significant differences were found among values.

Multilayer perceptron (MLP) is a neural network. For this analysis, we implemented a MLP that trains using a quasi-Newton algorithm which uses a backpropagation implementation of the gradient. We considered one hidden layer MLP with 20 neurons, ReLU (rectified linear unit) as activation function of the neurons and L-BFGS solver. This final setting has been defined after testing a combination of different values for the number of neurons of the hidden layer (10, 20, 40 and 80 neurons), the activation functions (ReLU, sigmoid) and the solvers (L-BFGS, Adam and RMSProp). The combination that gave the best results, in terms of classification accuracy average across subjects, was that used in this analysis.

Decision tree (DT) is a classifier which partitions the feature space until terminal nodes, each one assigned to a predicted value. Although decision trees are very easy to use for non-statisticians, they work for non-linear functions and the treatment of missing values is more satisfactory than most other model classes, we might not be able to find the best model at all. Moreover, results can be quite variable: small changes in the data can potentially lead to completely different splits (i.e. trees) [14].

Random Forest (RF) classifier is a set of decision trees merged by a probabilistic scheme. To classify an epoch, the corresponding feature vector is the input for each tree in the forest. Each tree makes a prediction and the forest chooses the prediction having the most votes over all the trees in the forest. RF can work on high-dimensional data and it can be applied to any model. Despite of its ability to returns the variable importance, it is very hard to interpret [14].

Many variant RF parameters impact on the algorithm accuracy. For each subject, we tested both the number of trees (10, 20, 50, 100, 200, 500, 1000, 2000) and the minimum number of samples required to split an internal node (from 2 to 24 in steps of two). The best set in terms of accuracy average (across subjects) was considered for

the following analysis: 2000 trees and 4 samples required to split an internal node.

Validation: A 10-times cross-validation (Fig. 1) was implemented to compare classifiers and number of features. For each iteration the feature domain (epochs x number of features, at most 240×120) was shuffled along the first size (epochs). The first ninety and the last ten percent of the data have been the training and testing dataset, respectively.

Training dataset was the input for the feature selector (RFE-CV based on DT). It performed the feature selection ten times using the same dataset and returned the list of features sorted according to the more selected among the feature selection iterations.

The first two or ten features were considered to reduce the feature domain or all features if feature selection was not required.



Figure 1: Validation approach. For each iteration (10 in total) the steps in the hatch block were repeated. Specifically, feature domain was shuffled and divided in training and testing dataset. The former was used to train the classifier (and to select the best two or ten features, if that was the condition under investigation), the latter to test the classifier. The performance index was computed for each iteration.

The feature domain, properly reduced (only for 2 or 10 features analysis), was the input for each classifier. Each classifier was trained from the training dataset. The testing dataset, never seen before, was used to test the model and compute the performance index.

For each pair number of features-classifier (e.g. 2 features – MLP) the average of the performance index across all iterations (10 in total) has been considered the emblematic value for that pair.

Performance Measures: For each pair number of features (2, 10, 120 features) and classifier (SWLDA, sLDA, LR, SVM, MLP, DT, RF) classification accuracy was computed.

Statistical Analysis: For each pair number of features-classifier the Shapiro-Wilk test was applied to assess the normality of each performance index distribution. To investigate the effect of the number of features as well as of the classifier and their potential interaction, classification accuracy was analysed by the repeated measure two-way analysis of variance (ANOVA). The Tukey HSD post hoc analysis was applied to assess pairwise differences. The threshold for statistical significance was set to $p < 0.05$. Results are presented as mean \pm standard error (SE) across subjects.

RESULTS

The statistical analysis revealed the significant effect of the classifier factor ($F=77.22$, $p < 0.001$) as well as the number of the features ($F= 19.11$, $p < 0.001$) on the classification accuracy and the significant interaction among factors ($F= 13.20$, $p < 0.001$).

Figure 2 shows for each pair (classifier-number of features) the results, presented as average and standard error across subjects.

The post-hoc analysis, applied to the *classifier* factor, pointed out the overall superiority of the SWLDA classifier over all classifiers as well as better performance obtained by the sLDA respect to those of the LR, SVM, MLP and DT classifiers. All classifiers outperformed DT classifiers.

Moreover, better performances were globally (*number of features* factor) achieved when ten or all available features were used than those obtained for two features. Since the number of features directly impacts on the number of physical EEG electrodes required to collect EEG data and, therefore, extract the needed features, results from interaction between classifiers and number of features were deeply analysed and reported in Fig. 3. With equal number of features (both for 2 and 10 features), SWLDA (accuracy average= 0.78 evaluated for 2 features, accuracy average= 0.79 evaluated for 10 features) statistically outperformed all classifiers. DT classifier, instead, (accuracy average= 0.62 evaluated for 2 features, accuracy average= 0.67 evaluated for 10 features) did not reached good performance, revealing to be the worst classifier (Fig. 3 upper panel, left side).

When all available information were used to train the classifiers, no statistically significant differences emerged among SWLDA, sLDA and RF (Fig. 3 upper panel, right side).

Increasing the size of the feature domain significantly improved performances in both sLDA (0.70, 0.75, 0.80 accuracy average for 2, 10 and 120 features) and RF classifiers (0.67, 0.73, 0.80 accuracy average for 2, 10 and 120 features). Conversely, SWLDA performances (0.78, 0.79, 0.80 accuracy average for 2, 10 and all features) did not differ among them varying on feature number.

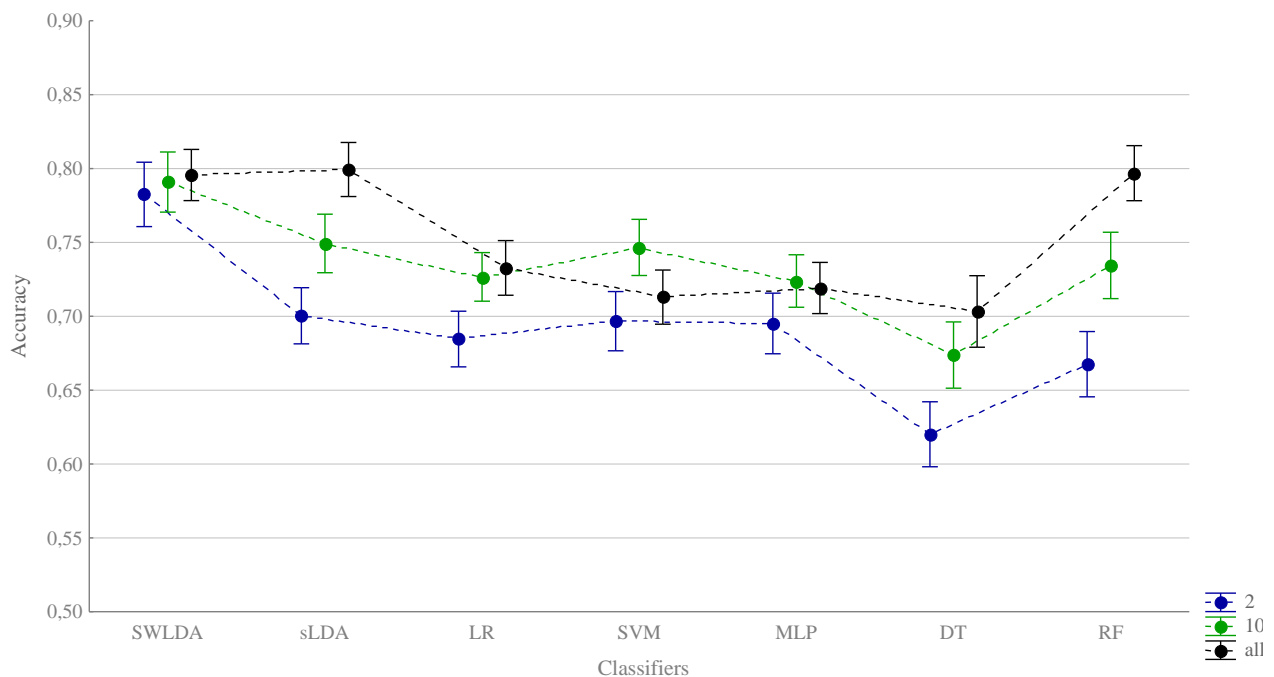


Figure 2: Classification accuracy, presented as mean \pm standard error (15 stroke patients), computed for seven classifiers: stepwise linear discriminant analysis (SWLDA), shrinkage linear discriminant analysis (sLDA), logistic regression (LR), support vector machine (SVM), multilayer perceptron (ML), decision tree (DT), random forest (RF). For each classifier, accuracy was evaluated when the feature domain had been reduced to include two features (in blue), ten features (in green) and all available (black) features, i.e. no feature domain dimensionality reduction.



Figure 3: Post-hoc test results of the ANOVA interaction factor. Upper panel, left side: comparison among classifiers with the same number of features. Pairwise differences among classifiers, for 2 and 10 features, were presented in same matrix since they had returned equal results. Upper panel, right side: comparison among classifiers when all features were considered. Lower panel, left side: comparison between classifiers trained from 2 features and those trained from 10 features. Lower panel, centre: comparison between classifiers trained from 2 features and those trained from all available features. Lower panel, right side: comparison between classifiers trained from 10 features and those trained from all available features.

Matrix reading: The classifier in each column header statistically differed/ did not differ from the classifier reported in the row header. Significant/no-significant differences correspond to coloured/white boxes. Green (orange) boxes means that the classifier in the column (row) header outperformed that in the row (column) header.

The increasing trend in accuracy was observed also for LR, DT and MLP classifiers: for the first the increase from 2 to 10 or 120 features statistically improved classification accuracy, for the neural network model the trend was not supported by the statistical results. SVM seemed, instead, to be prone to overfitting (0.70, 0.75, 0.71 accuracy average for 2, 10 and 120 features).

Lastly, the cross-check between classifier and number of features revealed that even the best model of the sLDA and RF (120 features) did not significantly differ from the SWLDA based just on two or ten features (Fig. 3, lower panel, centre and right side). Therefore, even if sLDA and SWLDA are both linear and, therefore, interpretable models, the last reached comparable performance by means few features (i.e. 10 features, less than 10 EEG channels).

DISCUSSION

Identifying the optimal classification method, based on relevant features, fast and able to provide an interpretable model of the EEG reinforced pattern, is a milestone in post-stroke rehabilitation protocols supported by BCI technology. In contrast to other fields of application

where optimal cursor control is pursued, in a rehabilitation context the reinforcement of the proper sensorimotor activation in terms of both topographic and spectral characteristics is the main aim.

Spectral features belonging to the sensorimotor area of the affected hemisphere, in alpha and beta bands, were extracted from EEG data of 15 stroke subjects to compare seven classifiers in terms of classification accuracy. Performance was also analysed varying on the number of features considered in the feature domain.

Stepwise linear discriminant analysis (SWLDA) revealed being the best classifier even just considering two or ten features. Considering all available features (120 features) shrinkage linear discriminant analysis (sLDA) and random forest (RF) achieved good results and comparable to those of SWLDA. Nevertheless good results, linear models (SWLDA and sLDA), resulting from the linear combination of features properly weighted, are more interpretable than RF model.

In our approach, indeed, monitoring the cursor trajectory, feedback provided to the therapist and directly related to the combination of proper features, allows to explain single trial and rehabilitative session performances.

RF belongs to the bootstrap aggregating methods based

on decision tree classifiers and, although decision tree is the simplest model because the intuitive interpretation, the structure of the RF (in our case 2000 decision trees) decreases the interpretability of the model by the clinicians. Among linear models, instead, even if SWLDA and sLDA reached the same performance, SWLDA built the model by less than 120 features: in most cases, the embedded feature selection process, starting from the empty model, did not add all predictors to the model. Moreover, the interaction among ANOVA factors did not highlight differences between SWLDA, trained with two or ten features, and both sLDA and RF trained by all features.

The linearity, the interpretability and the possibility to achieve good classification results also thank to the embedded selection process (not covered by the nature of the other classifiers) yielded SWLDA to be considered the best classification approach in the rehabilitation context. Furthermore, the possibility to monitor EEG patterns to reinforce by means few electrodes (10 features i.e. less than 10 EEG channels,) matches the use of BCI technology in clinical context.

Focusing for each classifier on the number of features factor, if from one hand for SWLDA the increasing trend, justified by the increasing number of features (2, 10, less than 120 features), was not supported by the statistical analysis, from the other hand the trend revealed being significant for both sLDA and RF. Moreover, with equal number of features, no differences were observed between sLDA and RF, supporting, therefore, the use of RF model as a good approach to the binary classification of motor imagery tasks, as proposed in [9]. Although Steyrl et al. observed the superiority (3% in accuracy) of the RF approach to the sLDA, the characteristics of their approach, i.e. different tasks, number of channels, pipeline of EEG signal processing, should be considered in the comparison. For similar reasons, our results did not confirm results in [5]. Although we used similar spectral features, the application of the common spatial pattern filter and the lower number of the recorded EEG channels may be the reason why the multilayer perceptron and the logistic regression did not show good performances.

CONCLUSION

SWLDA classifier statistically outperformed those commonly used in SMR-BCI paradigms, achieving good performance even in case of feature domain dimensionality reduction. Monitor the brain activity by means few EEG electrodes, indeed, is the key to use BCIs in clinical realm. Linearity, interpretability and impact on the usability yielded to positively evaluating SWLDA approach in the upper limb post-stroke motor recovery protocols supported by BCI.

ACKNOWLEDGEMENTS

We thank Angelica Cottarelli for support in the preliminary analysis of EEG data. This work was partially supported by the project APOSTROPHES,

Sapienza, University of Rome, Progetti di Ateneo and Promobilia Foundation (2018-H1 ref. 18076).

REFERENCES

- [1] Ramos-Murguialday A et al., Brain-Machine-Interface in Chronic Stroke Rehabilitation: A Controlled Study, *Ann. Neurol.*, vol. 74, no. 1, pp. 100–108, Jul. 2013.
- [2] Pichiorri F et al., Brain-computer interface boosts motor imagery practice during stroke recovery, *Ann. Neurol.*, vol. 77, no. 5, pp. 851–865, 2015.
- [3] Lotte F, Congedo M, Lécuyer A, Lamarche F, and Arnaldi B, A review of classification algorithms for EEG-based brain-computer interfaces, *J. Neural Eng.*, vol. 4, no. 2, pp. R1–R13, Jun. 2007.
- [4] Lotte F et al., A review of classification algorithms for EEG-based brain-computer interfaces: a 10 year update, *J. Neural Eng.*, vol. 15, no. 3, p. 031005, Jun. 2018.
- [5] Bashashati H, Ward RK, Birch GE, and Bashashati A, Comparing Different Classifiers in Sensory Motor Brain Computer Interfaces, *PLOS ONE*, vol. 10, no. 6, p. e0129435, Jun. 2015.
- [6] Colamarino E, Pichiorri F, Schettini F, Martinoia M, and Matti D and Cincotti F, Guider: A Gui for Semiautomatic, Physiologically Driven Eeg Feature Selection for a Rehabilitation Bci, *Proc. 7th Graz Brain-Comput. Interface Conf. 2017 Vis. Real.*
- [7] Krusienski DJ et al., A comparison of classification techniques for the P300 Speller, *J. Neural Eng.*, vol. 3, no. 4, pp. 299–305, Dec. 2006.
- [8] Krusienski DJ, McFarland DJ, and Wolpaw JR, Value of amplitude, phase, and coherence features for a sensorimotor rhythm-based brain-computer interface, *Brain Res. Bull.*, vol. 87, no. 1, pp. 130–134, 2012.
- [9] Steyrl D, Scherer R, Faller J, and Müller-Putz GR, Random forests in non-invasive sensorimotor rhythm brain-computer interfaces: A practical and convenient non-linear classifier, *Biomed. Tech.*, vol. 61, no. 1, pp. 77–86, 2016.
- [10] McFarland DJ, Lefkowitz AT, and Wolpaw JR, Design and operation of an EEG-based brain-computer interface with digital signal processing technology, *Behav. Res. Methods Instrum. Comput.*, vol. 29, no. 3, pp. 337–345, Sep. 1997.
- [11] Guyon I, Weston J, Barnhill S, and Vapnik V, Gene Selection for Cancer Classification using Support Vector Machines, *Mach. Learn.*, vol. 46, no. 1, pp. 389–422, Jan. 2002.
- [12] Bishop C, *Pattern Recognition and Machine Learning*. New York: Springer-Verlag, 2006.
- [13] 'LIBLINEAR -- A Library for Large Linear Classification'. [Online]. Available: <https://www.csie.ntu.edu.tw/~cjlin/liblinear/>.
- [14] Breiman L, *Classification and Regression Trees*. Routledge, 2017.