## A New Statistical Model of EEG Noise Spectra for Realtime, Low-γ-band SSVEP Brain-Computer Interfaces

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Introduction: A major impediment to practical real-time  $\gamma$ -band ( $\geq$  30Hz) SSVEP BCIs is the high level of spectral noise which dramatically increases the error rates of frequency detectors/estimators (Fig. 1a). The standard "1/*f*-type" spectral model [1] of EEG noise is both theoretically unsatisfactory and too ill-defined for hypothesis tests. Based on our new theory of *quantum ion channel kinetics* [2], we model EEG noise spectra as random processes of the form  $S_{\text{EEG}}(f) = S_{\text{GVZM}}(f) \cdot \Xi(f)$ , where  $\Xi(f)$  are independent  $\chi^2(2)/2$  random variables at each frequency f and  $S_{\text{GVZM}}(f)$  is the generalized van der Ziel-McWhorter deterministic function whose inverse Fourier transform is  $R_{\text{GVZM}}(t) = P_0 \int_{\tau_1}^{\tau_2} (1/\tau^{\alpha}) e^{-t/\tau} d\tau + P_1 \delta(t)$  for tunable parameters  $\alpha, \tau_1, \tau_2, P_0, P_1$  (Fig. 1b). We show such noise models have superior statistical characteristics for BCI and other neuroengineering applications.



*Figure 1.* (a) Raw single-trial EEG spectrum from 28Hz SSVEP BCI experiment showing a response peak which is nearly indistinguishable from background noise. (b) Synthetic GVZM  $\cdot \chi^2(2)/2$  noise spectrum optimally-fitted to the data of (a).

Figure 2. (a) Critical levels for SSVEP detection/estimation using standard smoothed periodogram algorithm [4] and the data of Fig.1. (b) Detection/estimation using optimally-fitted  $GVZM \cdot \chi^2(2)/2$  statistics.

*Material, Methods and Results:* The model was tested on a 15-second, 28Hz SSVEP trial (Fig. 1a) from a publically-available BCI dataset [3]. Biosemi electrodes A14-A16, A21-A23, A25, A27-A29 were averaged to form a virtual visual electrode. Blink artifacts were estimated by linear regression onto the three frontal electrodes. A popular *F*-test SSVEP detection algorithm [4] was compared to the same algorithm with its prestimulus estimator replaced by our optimally-fitted GVZM  $\cdot \chi^2(2)/2$  statistic. Each spectral value (excluding mid- $\alpha$ - and low- $\beta$ -bands) was classified with respect to its *F*-test critical value calculated from the null hypothesis

of no stimulus at that frequency. The results are shown in Fig. 2.

*Discussion:* The standard algorithm [4] failed to detect the 28Hz response spike in the noise background and also produced numerous false positives (Fig. 2a). On the other hand, our GVZM-based algorithm not only accurately detected the 28Hz response with P < .005, it also produced far fewer false positives (Fig. 2b).

Significance: This work proves that it is feasible to detect/estimate low- $\gamma$ -band SSVEP spikes in real-time despite their poor signal-to-noise characteristics by using neurologically-appropriate statistics for EEG background noise. Such noise models will be essential for the development of future practical real-time SSVEP BCIs in the mid- $\gamma$ -band.

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## References

- Destexhe A, and Rudolph-Lilith M., *Neuronal Noise*, Springer Series in Computational Neuroscience, Vol. 8. Springer, 2012.
   Paris A, Atia G, Vosoughi A, Berman S. Formalized quantum stochastic processes and hidden quantum models with applications to neuron ion channel kinetics, [Online], 2015, Available: http://arxiv.org/abs/1511.00057.
- [3] Bakardjian H, Tanaka T, Cichocki A., Optimization of SSVEP brain responses with application to eight-command brain computer interface, *Neurosci Lett.*, 469(1):34–38, 2010. [Online]. Available: http://www.bakardjian.com/work/ssvep\_data\_Bakardjian.html .
  [4] Liavas AP, Moustakides GV, Henning G, Psarakis E, Husar P. A periodogram-based method for the detection of steady-state visually evoked potentials, *IEEE Trans. Biomed. Eng.*, 45: 242–248, Feb. 1998.